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# Selected static characteristics of a parallel active power filter with feedback from the supply voltage

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**Abstract:** The article presents selected static characteristics of a parallel active filter with voltage control in the supply line (VPAPF – Voltage-controlled Active Power Filter) as a function of parameters of the supply network. The tests were done on the basis of a simulation model of the supply network and an appropriate compensator. The test results showed that VPAPFs are most suitable for operation in weak networks, maintaining an almost constant level of voltage distortion, regardless of the value of the network impedance. In addition, the influence of the parameter  $G$  corresponding to the conductance value suppressing higher harmonics of the network voltage on the operation of the active power filter was determined.

**Key words:** active power filters, distorted waveforms, harmonic compensation, higher harmonics, mathematical modelling, power quality, voltage deformation

## 1. Introduction

Active Power Filters (APF) are a well-known tool for suppressing higher harmonics in current and voltage waveforms [1–5]. For practical reasons industry usually uses Parallel Active Power Filters (PAPF), i.e., those in which the converter is connected in parallel to the load. These systems are designed primarily to suppress higher harmonics in the waveforms of current drawn from the network by a non-linear load. In addition, they can compensate for reactive power, as well as the asymmetry of the three-phase energy receiver (“seen” from the network side) [1–4, 6, 7]. However, with traditional control (i.e., one in which the compensating for current waveforms is determined on the basis of identifying the supply current distortions), such filters are not able to compensate for disturbances coming from the powering side [8–13]. The solution to this problem



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is to use parallel active power filters also called conductance-controlled filters, whose control is based on the identification of grid voltage distortions at the point of common coupling (PCC) (Voltage-controlled Parallel Active Power Filter, VPAPF), [1, 3, 10–30]. Some publications also use the term “virtual resistance/conductance circuit” [27, 28, 32]. Such controlled active power filters behave like selective conductance [27, 28], the value of which is low for the fundamental harmonic of the supply voltage, and relatively high (equal to the  $G$  value) for higher order harmonics. The idea of controlling such a compensator is shown in Fig. 1.

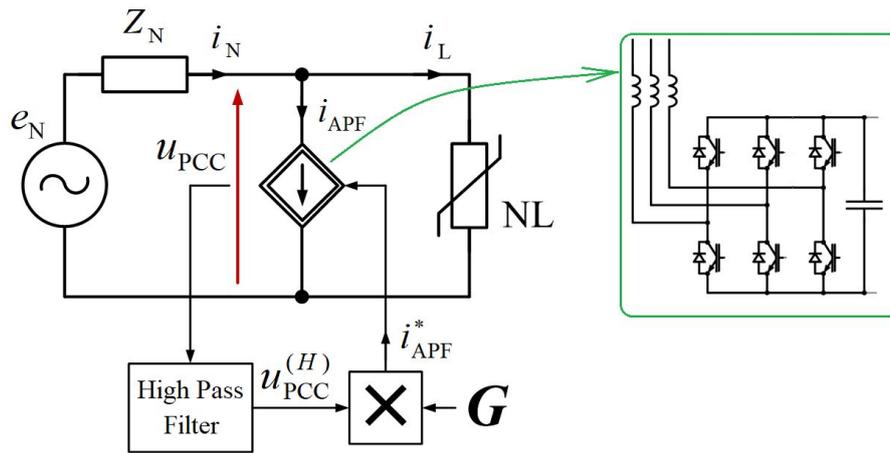


Fig. 1. Conceptual, simplified diagram of a parallel active filter with voltage control in the supply line:  $e_N$  – equivalent network voltage (Thevenin voltage),  $Z_N$  – equivalent network impedance (Thevenin impedance), NL – nonlinear load

The reference current  $i_{APF}^*(t)$  to be introduced by the compensator into the considered node is determined from the following relation:

$$i_{APF}^*(t) = G \cdot u_{PCC}^{(H)}(t), \quad (1)$$

where:  $u_{PCC}^{(H)}(t)$  is the harmonic component of the supply voltage waveform at the Point of Common Coupling (PCC),  $G$  is the active filter gain (equal to the value of selective conductance). The controlled source shown in Fig. 1 is in fact a power electronic converter controlled in such a way as to introduce a given current waveform  $i_{APF}$  to the PCC node.

Figure 2 shows a complete control algorithm for such an active filter. The phase (or interphase) voltage waveforms  $u_{PCC\ ABC}$  are transformed into a dq coordinate system rotating with the fundamental harmonic pulsation. Then, the harmonic component of this voltage  $u_{PCC\ dq}^{(H)}$  is isolated by the high-pass filter and after multiplying it by the value of the virtual conductance  $G$ , a reference current waveform  $i_{dq}^*$  is obtained. This current is supplemented with the  $\Delta i_d^*$  component determined by the PI controller in order to stabilize the voltage in the DC bus of the converter (to compensate for losses in the converter). After returning to the static coordinate system  $\alpha\beta$ , the current regulator (i.e., Dead-Beat) generates the signal waveform of the given voltage  $u_{APF\ \alpha\beta}^*$  and then, the SVPWM modulator generates gating signals to switch the power transistors of the converter.



of 50 m $\Omega$ . The capacitance of the capacitor  $C_{sh}$  shunting the active power filter (necessary for such a controlled compensator [16–18, 28]) was 470  $\mu$ F (in each phase), and taken into account, the capacitor's equivalent series resistance  $R_{sh}$  was 5 m $\Omega$ . In such a system, the steady-state behavior of the considered active power filter was tested at different values of the network impedance  $Z_N$  parameters and at different values of the active power filter gain  $G$ .

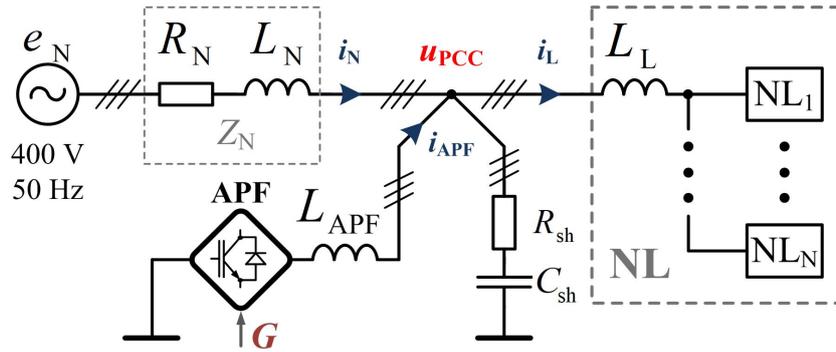


Fig. 3. Diagram of a low-voltage power network with a non-linear load and a voltage-controlled parallel active power filter (VPAPF) used for determining static characteristics

The simulation tests were divided into two parts. In the first part, the equivalent resistance  $R_N$  and the equivalent reactance  $X_N$  of the network, occurring from the power supply side at the PCC clamps, were changed independently, wherein the reactance value was determined for the fundamental harmonic and from now on it will be understood in this way. The resistance value was changed from 50 m $\Omega$  to 1  $\Omega$  in 50 m $\Omega$  steps, while the reactance value was changed from 0  $\Omega$  to 1  $\Omega$  with the same steps. As a result, for each determined characteristic, 420 points were obtained. All points were obtained with a constant gain value of  $G = 6$ . This value was large enough to ensure satisfactory harmonic compensation, and, at the same time, it guaranteed a safe margin of stability. On the basis of the above assumptions, a number of static characteristics was determined, showing the relation between the selected physical quantities occurring at the considered PCC point as a function of resistance and reactance of the supply network. Then, in the second part of the tests, the influence of the gain  $G$  value and the equivalent network impedance  $Z_N$  on the performance of the considered active power filter was examined. Since the presentation of the characteristics in the function  $G$ ,  $R_N$  and  $X_N$  would require the use of four dimensions, the representation of the characteristics was limited to the impedance module  $|Z_N|$ , assuming equality as to the values of the  $R_N$  and  $X_N$  parameters. Both quantities were changed from 50 m $\Omega$  to 1  $\Omega$  in 50 m $\Omega$  steps. In turn, the gain value  $G$  was changed from 0 to 10 in steps of 0.5. On the basis of the above assumptions, a number of static characteristics were determined, showing the relation between the selected physical quantities occurring in the considered PCC point as a function of the gain  $G$  and the value of the impedance module  $|Z_N|$ .

The value at each point of each obtained characteristic was determined as the arithmetic average of one hundred values calculated from one hundred following periods of the supply voltage waveform in a steady state.

## 2.1. Obtained static characteristics as a function of equivalent resistance $R_N$ and reactance $X_N$ of the supply network

In order to determine the reference levels needed for further analysis, the characteristics  $THD(U_{PCC}) = f(R_N, X_N)$  for the network in Fig. 3, however, operating without a compensator was determined first. The PN-EN 50160 standard provides for the analysis of harmonics up to and including the 40-th order [35]. However, due to the fact, that converter systems can introduce components with much higher frequencies (e.g., carriers), and also due to the phenomena shown later in the article, the calculations were made for a much wider frequency bandwidth. The characteristics made on this basis are shown in Fig. 4.

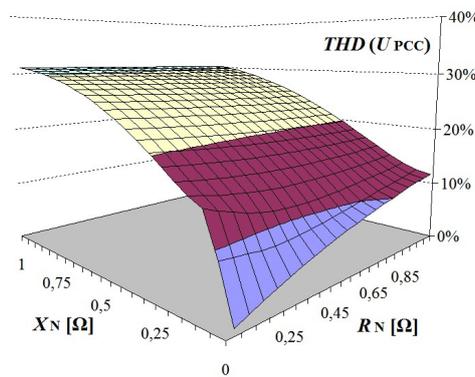


Fig. 4. Static characteristics showing the  $THD$  of the supply voltage at the PCC point, for various values of equivalent resistance and reactance of the low voltage supply network in the absence of a compensator

With the network impedance close to zero, voltage distortions are small. With the increase in the resistance  $R_N$  up to a value of  $1 \Omega$  and with the zero-reactance  $X_N$ , the harmonic distortion of the supply voltage with the applied load NL increases to 11.9%. With the increase in network reactance up to a value of  $1 \Omega$ , the voltage distortion also increases to 31.0%. With a reactance equal to  $100 \text{ m}\Omega$  and a resistance not exceeding  $200 \text{ m}\Omega$ , the fluctuation of the discussed characteristic is noticeable. It is caused by the nature of used non-linear NL load composed of several different non-linear energy receivers, which propagates the greatest disturbances at this network impedance value and in the considered case has a particular influence on increasing the contribution of the 5-th harmonic.

Next, the VPAPF was connected to the PCC node and the tests were repeated. As their result, another characteristic was obtained (Fig. 5). With a low network impedance, the supply voltage distortions are almost non-existent. However, with an increase in the value of this impedance, the voltage  $THD$  increases slightly. The active filter effectively suppresses unwanted frequency components, keeping the harmonic distortion at a level not exceeding 3.03%. A further increase in both the equivalent resistance and the reactance of the power network does not cause significant changes in the voltage  $THD$  value, which is a special, and so far, unknown advantage of parallel active filters controlled in this way.

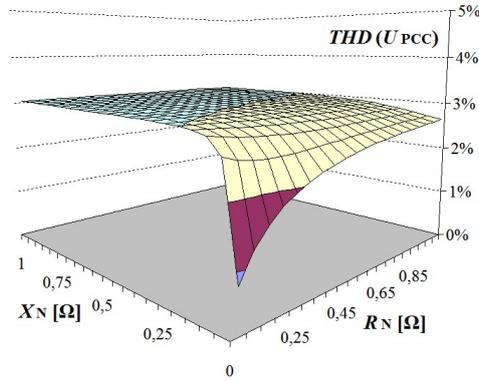


Fig. 5. Static characteristics showing the  $THD$  of the supply voltage at the PCC point for various values of equivalent resistance and reactance of the low voltage supply network after connecting the compensator

For better visualization of the positive influence of the VPAPF on the power quality and to highlight its role in the modeled network, the distortion attenuation coefficient  $k$  was introduced. It was defined as the quotient of the voltage  $THD$  factor at a selected PCC node in the absence of the compensator, to the value of this factor at the same node in the presence of the compensator:

$$k = \frac{THD(U_{PCC})|_{\text{without APF}}}{THD(U_{PCC})|_{\text{with APF}}} \quad (2)$$

This coefficient carries information about the multiplicity of reducing the distortion of the voltage waveform in the considered PCC node after engaging the VPAPF. The characteristics illustrating the value of the coefficient defined in this way for various network resistance and reactance values are shown in Fig. 6.

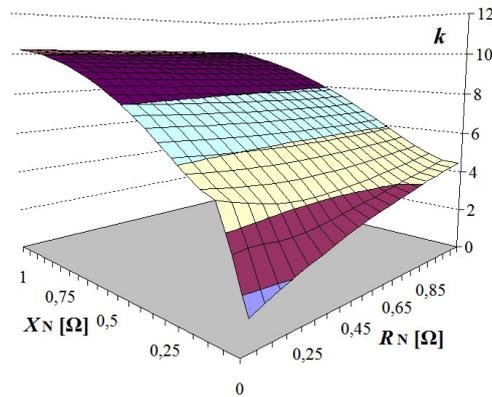


Fig. 6. Static characteristics showing the value of the voltage distortion attenuation coefficient  $k$  for various values of the equivalent resistance and reactance of the low voltage supply network

For a very low network impedance value (so, practically, with no voltage distortion), the active power filter does not generate significant compensating currents. For this reason, the  $k$ -coefficient values are close to unity. With increasing network resistance value (and with zero reactance), the value of the distortion attenuation coefficient increases and at  $R_N = 1 \Omega$ , the  $k$  equals 4.50. A similar tendency causes an increase in the network reactance value. With almost zero network resistance and  $X_N = 1 \Omega$ , the voltage waveform shape improves 10.2 times. Alike filtration efficiency occurred at the maximum considered values of network resistance and reactance, where the multiplicity of voltage distortion attenuation was 10.0.

Characteristics  $k = f(R_N, X_N)$  show another important advantage of active filters controlled according to the proposed algorithm, namely, their effectiveness increases with the increase in network impedance (so with the increase in susceptibility of this network to voltage distortions, in contrast to conventionally controlled parallel active filters [12, 13]). This relation determines the applicability range of VPAPF systems in very weak power grids.

The characteristics of the current root-mean-square (rms) value introduced by the compensator to the PCC as a function of both components of the network impedance,  $I_{APF\ RMS} = f(R_N, X_N)$ , were also determined (Fig. 7). For impedance close to zero, the active power filter injects a negligible compensating current due to small distortions of the supply voltage. However, with a slight increase in the  $X_N$  value (starting from 50 mΩ), further increase in the resistance value  $R_N$  results in the injection of the compensating current  $I_{APF}$  into the PCC with an increasingly smaller rms value. This happens e.g., because with the increase in network impedance, due to the increasing voltage drop on this impedance, the value of the supply voltage  $U_{PCC}$  decreases, both its fundamental harmonic and the harmonic component  $U_{PCC}^{(H)}$ . The latter component is the basis for determining the reference compensating current  $i_{APF}^*$  (Fig. 1), according to expression (1).

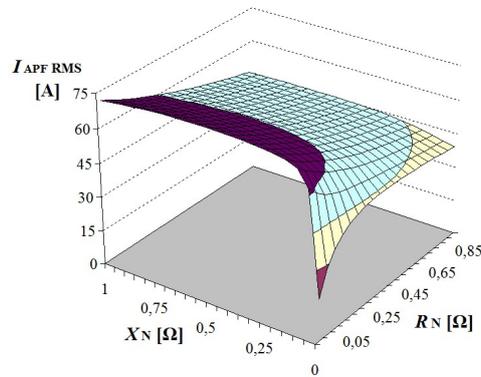


Fig. 7. Static characteristics showing the rms value of the compensating current introduced to the PCC by the active power filter for various values of equivalent resistance and reactance of the low voltage supply network

To designate the utilization level of the compensation current injected by the compensator to the PCC node (in order to improve the shape of the voltage waveform), another auxiliary factor was introduced. It was defined as the quotient of the distortion attenuation coefficient  $k$  to the compensating current ( $k/I_{APF\ RMS}$ ), which was injected into the node, causing a  $k$ -fold decrease in the voltage deformation in this node. The characteristic (Fig. 8) showing this coefficient informs

about the efficacy of compensation for each ampere of the current  $I_{APF}$  injected to the PCC as a function of the supply network resistance and reactance. Apart from inappreciable fluctuations at low values of the network impedance, this characteristic is increasing until the end of the considered range. This means, that with the increase in network impedance, the compensating current  $I_{APF}$  introduced to the node by the compensator is used more effectively.

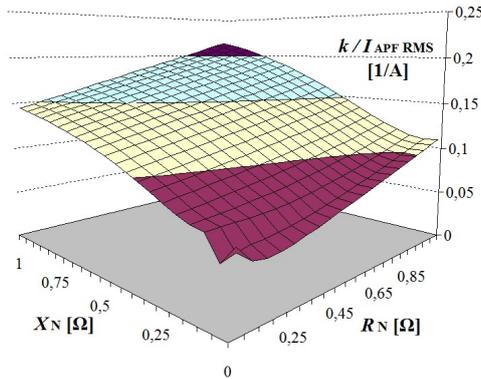


Fig. 8. Static characteristics showing the efficacy level of use of the compensating current for various values of equivalent resistance and reactance of the low voltage power supply network

## 2.2. Obtained static characteristics as a function of gain $G$ and supply network impedance module $|Z_N|$

Figure 9 shows the characteristic  $THD(U_{PCC}) = f(G, |Z_N|)$ . For a zero value of gain  $G$ , the active power filter does not generate the compensating current  $I_{APF}$  (so it is practically an open circuit at its clamps). Increasing the value of  $G$  results in a visible suppression of higher harmonics

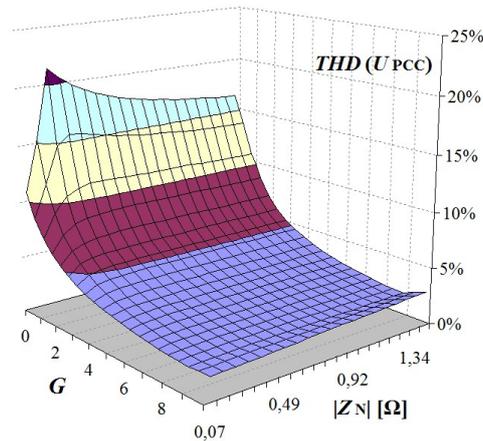


Fig. 9. Static characteristics showing the  $THD$  of the supply voltage at the PCC node for various values of the gain  $G$  and the module of the equivalent impedance of the low-voltage supply network  $|Z_N|$

in the supply voltage UPCC, reducing the *THD* to 2.002%. However, after exceeding a value of 8.5 for this parameter, the harmonic distortion starts to increase insignificantly. It is visible in Fig. 8, especially for higher values of the network impedance modulus  $|Z_N|$  (over  $0.49 \Omega$ ). This is because higher gain values bring the system closer to the boundary of the stability margin area. This results in generating oscillations by the active power filter. A further increase in  $G$  would result in a definite loss of stability of the compensator.

The next characteristic, presented in Fig. 10, illustrates the function of the previously defined distortion attenuation coefficient  $k = f(G, |Z_N|)$ . An increase in the network impedance module results in an increase in the value of this coefficient. Increasing the gain  $G$  to the value of 8.5 also increases the value of the  $k$  coefficient, in this case a 13.4-fold improvement in the supply voltage waveform shape was noted. Further increasing the  $G$  parameter above a value of 8.5 results in a rapid decrease in the voltage distortion attenuation factor  $k$  (from 13.4 to 10.0) due to the oscillations introduced by the compensator, which initiate a loss of stability.

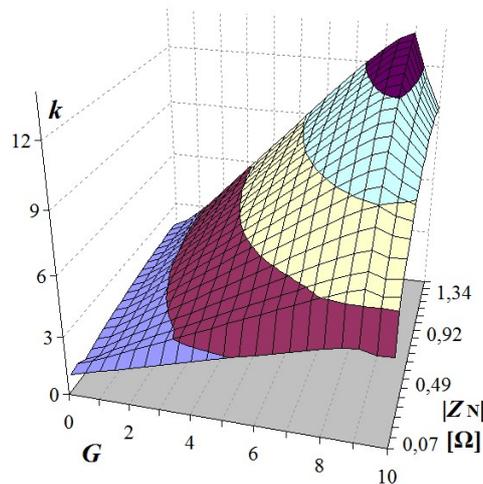


Fig. 10. Static characteristics showing the value of the voltage deformation attenuation coefficient  $k$  for various values of the gain  $G$  and the module of the equivalent impedance of the low voltage supply network  $|Z_N|$

In the considered system, these oscillations occurred in the band over 2 kHz. This argument supports the legitimacy of conducting the analysis not only in the range of harmonics provided for in the PN-EN 50160 standard [35], but in justified cases in the widest possible band, at least up to the switching frequency of the converter transistors in the power circuit of the compensator [34] (which was done in this study). Therefore, one must be careful not to introduce additional parasitic harmonics when using a filter.

For the considered system, a characteristic showing the rms value of the harmonic component of the supply  $U_{PCC}^{(H)} = f(G, |Z_N|)$  was also determined (Fig. 11). Ideally, this value would be reduced to zero. In practice, it is satisfactory to reduce this component to a value of 8% of the fundamental harmonic for public networks [35], which in the considered case is already at  $G = 2$ . The noticeable feature of this characteristic is that as the gain increases, the steepness of the characteristic in the direction of the  $G$  axis (module of derivative  $dU_{PCC}^{(H)}/dG$ ) decreases. Therefore,

the operation with a too high gain value is not always energetically reasonable. In turn, the increase in the value of  $U_{\text{PCC}}^{(H)}$  at  $G \geq 8.5$  visible in the characteristics is caused by the oscillations discussed earlier, which are introduced by the VPAPF.

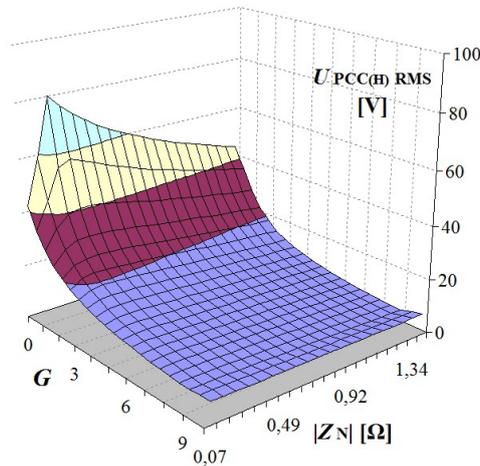


Fig. 11. Static characteristics showing the supply voltage harmonic component rms value for various values of the gain  $G$  and the module of the equivalent impedance of the low voltage supply network  $|Z_N|$

The characteristic of the rms value of the compensator current  $I_{\text{APF RMS}} = f(G, |Z_N|)$  is shown in Fig. 12. It tends to decrease with increasing network impedance. However, as the gain increases, the steepness of this characteristic along the  $G$  axis decreases, which means (as in the case above) that operating with too high a gain value is not always reasonable. In addition, an increase in  $G$

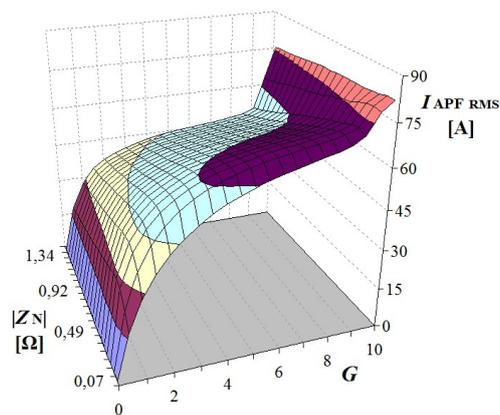


Fig. 12. Static characteristics showing the compensating current rms value introduced to the PCC by active power filter for various values of the gain  $G$  and the module of the equivalent impedance of the low voltage supply network  $|Z_N|$

above 8.5 results in a rapid increase in the rms value of the compensating current. This is caused by the appearing oscillating component, heralding the risk of stability loss.

The last static characteristic obtained during the tests shows the previously defined compensation current utilization coefficient  $k/I_{\text{APF RMS}}$  (Fig. 13). This characteristic reveals some fluctuations for small values of the network impedance module  $|Z_N|$ . However, with  $|Z_N|$  increase, the value of the compensation current utilization coefficient increases. A similar tendency occurs in the gain function. With increasing  $G$ , the characteristic also initially increases, but after exceeding a value of 8.5 there is a very rapid decrease in value due to the appearance of oscillations.

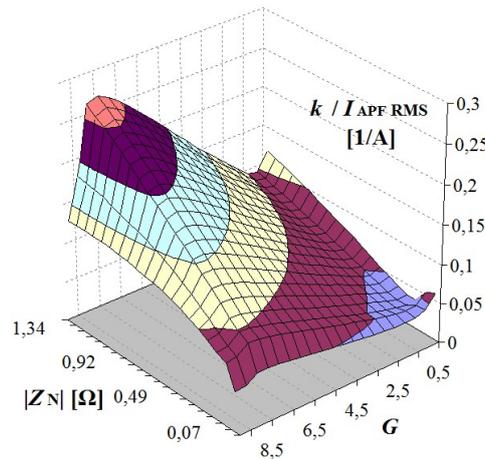


Fig. 13. Static characteristics showing the efficacy level of use of the compensating current for various values of the gain  $G$  and the module of the equivalent impedance of the low voltage supply network  $|Z_N|$

Thus, too high a gain value results not only in the deterioration of the voltage waveform shape (by introducing an unnecessary oscillating component) but also leads to a very high load (and the risk of overload) of the converter's power circuit.

### 3. Conclusions

As the research shows, active power filters controlling voltage in the powering line have features that determine the scope of their applicability. One of such features is the fact that VPAPFs are able to maintain an almost constant level of harmonic distortion in the supply voltage, regardless of the equivalent value of the network impedance  $Z_N$ , working with a constant value of the gain  $G$  (in the conducted research, the gain was 6). This is illustrated by the characteristics in Fig. 5. Additionally, in relatively weak networks (with the value of the equivalent impedance  $|Z_N|$  larger than  $0.1 \Omega$ ), with a further increase of  $|Z_N|$ , the demand for the rms value of the compensating current, needed to maintain the voltage  $THD$  at a reduced (constant) value, decreases (Fig. 12 along the  $|Z_N|$  axis for  $|Z_N| > 0.1 \Omega$ ). Note, that for the value  $|Z_N|$  lower than  $0.1 \Omega$ , the considered network is relatively strong, so there is practically nothing to compensate. Hence the

small  $I_{APF\text{ RMS}}$  values in the characteristic area close to the origin of the coordinate system in Fig. 7. The same characteristics show that the tendency of lower demand for compensating current mentioned above is influenced particularly by the network resistance  $R_N$  (Fig. 7 along the  $R_N$  axis for  $X_N$  larger than  $0.1\ \Omega$ ). Moreover, with the increase in the network impedance, the value of the compensation current utilization coefficient  $k/I_{APF\text{ RMS}}$  increases (Fig. 13). This makes the proposed active filters perfectly suitable for the compensation of higher voltage harmonics in weak networks, and their implementation in such networks allows the use of smaller (cheaper) elements to build a power electronics converter circuit. The gain  $G$ , corresponding to the value of conductance shunting unwanted voltage harmonic components in the PCC node, is an essential parameter that allows influencing the intensity of harmonic suppression and the apparent power with which the compensator affects the supply voltage waveforms in the considered node. The relation between gain and filtration effectiveness is not linear (each multiplication of the  $G$  value improves the voltage shape by a correspondingly smaller multiplicity), but in most cases it is satisfactory to reduce the level of voltage distortion to 8%, taking into account only 40 first harmonics [35]. Therefore, working with too high gain values is usually unjustified, not only from the energy and economic point of view, but also because of the risk of oscillation and even loss of stability (Fig. 9–13). What is worse, these oscillations may have a higher frequency than the highest harmonic provided for by the standard PN-EN50160 [35] (which was the case in the presented example, Fig. 4, 5), therefore, in the case of using an active power filter, it is reasonable to conduct spectral analysis in a much wider frequency bandwidth [34].

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